

Comparison of Hydrogen (H) and Helium (He) Spectra

We know that for hydrogen atom the expression of wavelength is given as.

$$\frac{1}{\lambda} = R_m Z^2 \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right), \text{ where } R_m \text{ is Rydberg Constant}$$

for Hydrogen atom $Z = 1$,

$$\frac{1}{\lambda} = \mathcal{V} = R_H \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right) \text{ ————— (1)}$$

for Helium (He^+) $Z = 2$.

$$\frac{1}{\lambda} = \mathcal{V} = R_{He} 4 \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)$$

$$\boxed{\frac{1}{\lambda} = \mathcal{V} = 4 R_{He^+} \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right)} \text{ ————— (2)}$$

$n_f = 4$, $n_i = 5, 6, 7, \dots$ Pickering series
(near ultraviolet and visible)

$n_f = 3$, $n_i = 4, 5, 6, \dots$ Fowler series
(ultraviolet and visible)

$n_f = 2$, $n_i = 3, 4, 5, \dots$ Lyman series

A comparison of the Balmer series for R_H with

the Pickering series formula for R_{He^+}

$$\frac{1}{\lambda} = \nu = R_H \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right), \quad n_i = 3, 4, 5, \dots$$

and $\frac{1}{\lambda} = \nu = 4 R_{He^+} \left(\frac{1}{n_f^2} - \frac{1}{n_i^2} \right), \quad n_i = 5, 6, 7, \dots$

For H-atom

$$\frac{1}{\lambda} = R_H \left(\frac{1}{4} - \frac{1}{9} \right), \quad n_i = 3$$

$$\frac{1}{\lambda} = R_H \left(\frac{5}{36} \right)$$

$$\boxed{\frac{1}{\lambda} = \frac{5}{36} R_H}$$

For He^+

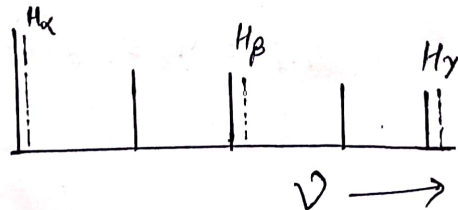
$$\frac{1}{\lambda} = 4 R_{He^+} \left(\frac{1}{16} - \frac{1}{36} \right), \quad n_i = 6$$

$$\frac{1}{\lambda} = 4 R_{He^+} \left(\frac{36 - 16}{16 \times 36} \right)$$

$$\frac{1}{\lambda} = \cancel{4} R_{He^+} \frac{\cancel{20} 5}{\cancel{16} \times 36}$$

$$\boxed{\frac{1}{\lambda} = \frac{5}{36} R_{He^+}}$$

Comparison shows that alternate member of the Pickering series $n_i = 6, 8, 10, \dots$ must coincide with members $n_i = 3, 4, 5$ of the Balmer series provided $R_H = R_{He^+}$



A careful examination shows that Balmer lines of H-atom are not exactly coincident with alternate lines of the Pickering series of He^+ .

The small displacement between these lines is due to the difference in R_H and R_{He^+} which arises due to finite mass of the nucleus.

It is found that the series limits λ_{min} of Balmer and Pickering series differ by 11 cm^{-1}

Now for H.

$$(\nu_{\text{max}})_H = \frac{R_H}{2^2} \quad (n_i = \infty) \text{ Balmer series}$$

For He^+

$$(\nu_{\text{max}})_{\text{He}^+} = \frac{4 R_{\text{He}^+}}{4^2} \quad (n_i = \infty) \text{ Pickering series}$$

$$R_H = 4 \nu_{\text{max}}$$

$$R_{\text{He}^+} = 4 \nu_{\text{max}}$$

$$R_{\text{He}^+} - R_H = 4 [(\nu_{\text{max}})_{\text{He}^+} - (\nu_{\text{max}})_H]$$

$$(\nu_{\text{max}})_{\text{He}^+} - (\nu_{\text{max}})_H = 11 \text{ cm}^{-1}$$

$$R_{\text{He}^+} - R_H = 4 \times 11 \text{ cm}^{-1}$$

$$\boxed{R_{\text{He}^+} - R_H = 44 \text{ cm}^{-1}}$$